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Why Branded Firms May Benefit from Counterfeit Competition

Why Branded Firms May Bene t from Counterfeit Competition

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Abstract

A durable-good monopolist sells its branded product over two periods. In period 2, when there is entry of a counterfeiter, the branded rm may charge a high price to signal its quality. Counterfeit competition thus enables the branded rm to commit to a high price in period 2, alleviating the classic time-inconsistency problem under a durable-good monopoly. This can increase the branded rm's pro t by encouraging consumer purchase without delay, despite the revenue loss to the counterfeiter. Total welfare can also increase, because early purchase eliminates delay cost and consumers enjoy the good for both periods.

JEL: D82, L11, L13

Keywords: Counterfeit, Durable Good, Quality Signaling

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1 Introduction

Counterfeits have become a fast growing multi-billion dollars business. In the 2007 OECD counterfeit report, the volume of counterfeits was around 200 billion dollars in international trade, 2% of world trade.¹ This gure does not include domestic consumption of counterfeits or digital products distributed via internet. The U.S. government estimated that counterfeit trade increased more than 17 fold in the past decade (U.S. Customs and Border Protection 2008).

Counterfeits are generally viewed as harmful to both the authentic producers and consumers, especially when they are deceptive, such as counterfeits of pharmaceutical products, eyeglasses, luxury goods or even normal textile products of famous brands.². However, some recent empirical evidence suggests that (deceptive) counterfeits could actually bene t the branded rm. In particular, Qian (2008) nds that the average pro t for branded shoes in China is higher after counterfeit entry. Qian (2011) provides further evidence that the impact of counterfeits on pro t depends on the quality gap between the authentic good and the counterfeit good; the branded rm bene ts from counterfeits when the quality gap is su ciently large. In this paper, I provide a theoretical explanation of why a branded rm can indeed bene t

¹The Economic Impact of Counterfeiting and Piracy http://www.oecd.org/industry/ind/ 38707619.pdf

²This does not mean consumers cannot distinguish products at all. It is just hard for buyers to tell whether the good is authentic without any other information. For example, a consumer may not be able to separate a genuine Chanel bag from a fake one only by appearance. However, if one is priced at \$3,000 and the other is sold for \$50, she will know that the expensive one is more likely to be authentic ex post. On the other hand, non-deceptive counterfeits are those that consumers can easily recognize when purchasing, such as digital products.

products is large enough.

I consider a model with an authentic durable-good rm which sells in two periods. Without counterfeits, the branded durable-good monopolist faces the classic timeinconsistency problem (Coase, 1972): after selling to high-value consumers in the rst period at a high price, it cannot resist cutting its price in the second period. But then rational consumers will delay their purchase, forcing the monopolist to reduce its price in the rst period and lower the monopolist's overall pro t. Now suppose that a counterfeiter will enter the market in the second period. In order to separate its product from counterfeits, the branded rm needs to set a high price to signal its quality. Thus the presence of counterfeits enables the branded rm to commit to a high price in period 2, providing a solution to the time-inconsistency problem. This then motivates more consumers to purchase in period 1 instead of waiting to buy in period 2, even if the rst-period price is high. When the quality gap is su ciently large, this \front-loading" e ect will dominate the pro t loss from competition in the second period. In terms of total welfare, counterfeits are likely to decrease surplus in the second period; however, rst-period welfare increases due to front loaded purchases. Early purchases contribute twice the surplus compared to late purchases because consumers can use the good for two periods. Therefore, if the quality gap is not too large, it is possible for counterfeits to increase welfare.

The results in this paper shed light on the policy towards counterfeits. Both branded rms and consumers respond to counterfeits strategically. In the model, the authentic rm separates itself from the counterfeiter through high price when the quality gap is large enough. Therefore, consumers will not be fooled by counterfeits with extremely low quality. Moreover, knowing the later counterfeit entry, consumers are more inclined to purchase early, which bene ts both the authentic rm and total welfare in a dynamic context.

3

The existing literature has investigated varies strategies by the durable-good mo-

beginning of the game. However, they are not able to tell which good is produced by the branded rm from its appearance before their purchase.⁴ This contrasts with the standard assumption that consumers can trace the producer of the good.

There is a unit mass of heterogeneous consumer indexed by the taste parameter U[0; 1]. Consumer's utility has the linear function form:

$$U_i = {}_i Q_i$$
 p_i ; $i \ 2 \ fA$; Cg ; where p_i is the price of rm i

The discount factors of both rms and consumers are assumed to be 1.

Let $_i(p_A; p_C)$ be the probability that consumers believe the good from rm i is the authentic good, given p_A and p_C . Unlike the traditional monopoly signaling model, there are two signal senders here. Consumer belief is based on price and the number of rms charging that price. Consumers are aware that two rms sell the good and one of them is the counterfeiter. Thus, $_A(p_A; p_C) + _C(p_A; p_C) = 1$ in equilibrium. In a pooling equilibrium, where $p_A = p_C$, consumers cannot separate two products and $_A = _C = \frac{1}{2}$. In a separating equilibrium, where $p_A \notin p_C$, consumers believe that the expensive good is authentic and the cheap one is counterfeit.

Given consumer's belief, the rm's pro t is represented by

$$_{it}^{k}(p_{A}; p_{C}; i); t 2 f_{1}; 2g; k 2 f_{P}; Sg$$

The subscript *i*, *t* stands for rm type and time respectively. We use the superscript *k* to denote equilibrium values in the second period (P for Pooling Equilibrium and Sstuc28(th-2689tha

for Separating Equilibrium). Also, assume that the separating equilibrium is selected when pro ts are the same for a separating and a pooling equilibrium.

The time-line of the game is as follows: the authentic rm sets the rst-period price p_1 in t = 1. Consumers decide whether to buy or wait. The counterfeiter enters in t = 2 and both rms set prices simultaneously. Then consumers observe both prices and make a purchasing decision based on their beliefs.

Before analyzing the game with counterfeit competition, let's rst review the benchmark monopoly model without entry.⁵

(i) When the monopoly lacks commitment power, it has an incentive to decrease the price to reap the residual demand in t

This gives a optimal prot $=\frac{1}{2}$ and $_{1}=\frac{1}{2}$. The prot in no commitment case is lower because of the standard time-inconsistency problem: high valuation consumers will anticipate the price reduction in the future and some of them postpone purchase to the second period.

3 Equilibrium Analysis With Counterfeit Competition

In this section, I will rst characterize the set of Perfect Bayesian Equilibrium (PBE) under counterfeit competition. I then show that there exists an equilibrium at which the counterfeit can increase the authentic rm's pro t and social welfare.⁶

Standard backward induction is applied to analyze the counterfeit game. As in the benchmark, there is a marginal consumer $_1$, such that all consumers with taste parameter above $_1$ will purchase in the rst period. The remaining consumers may purchase in the second period. $_1$ can be interpreted as the market size of the second period.

3.1 Signaling Game in Second Period

In t=2, there is a signaling game played between a pair of vertically di erentiated rms and consumers. Consumers use market prices to update their beliefs. If both rms have the same price, counterfeits are indistinguishable ex post and a pooling equilibrium is sustained. If the counterfeiter sets a lower price than the branded rm and reveals itself, there will be a separating equilibrium where consumers know for

⁶In next section, I show all equilibria survive from the re nement have the desired result

products are close substitutes, the cost of signaling for the branded rm is so high that it would rather pool with the counterfeiter.

As in other signaling games, this model also has multiple equilibria. In some pooling equilibria with low price, counterfeit competition is detrimental to the branded rm's pro t. In this section, I will show that there exists an equilibrium in which both the authentic rm and the society bene t from counterfeit entry under certain conditions. In the next section, it is proved that all equilibria surviving from the Competitive Intuitive Criterion re nement have similar properties.

The equilibrium I will focus on here is the one with the highest second-period pro t for authentic rm, which is de ned as the **pro t-maximizing equilibrium**. It seems reasonable that consumers will believe that the authentic rm will choose the price that maximizes its second-period pro t. Therefore, consumers believe the rm charging that price is the authentic rm. If both rms set that price, the good has 50% probability to be genuine. Any other price indicates a fake product. This is the pessimistic belief that supports the pro t-maximizing price in t=2. Formally, consumer belief is de ned as follow.

$$i(p_{A2}; p_{A2}) = \frac{1}{2}; \quad A(p_{A2}; p_2) = 1; 8p_2 \notin p_{A2};$$
$$A(p_2;) = C(; p_2) = 0; 8p_2 \notin p_{A2}$$

In this section, an extra asterisk is used in superscript to denote variables in the pro t-maximizing equilibrium. Let p_{A2}^{S} and p_{2}^{P} be the authentic price in the optimal separating and pooling equilibriumd [(coubriu)1(md [(co(in)-d2a7g)-400ts(li7oter.)]277(0)]TJv4

of signaling game in t=2. $p_{A2} = p_{A2}^S = \underline{p_2}(1,C), \quad A_2 = \sum_{A2}^S = \frac{4(1-C)^2(1-C^2)}{C^2-3C+4} \frac{2}{1}$. (ii) If the counterfeit's quality is high $(C > C_3)$, the pooling equilibrium will be selected. (a) For $C_3 < C$ C_2 0:702, $p_2 = p_2^P = \frac{1+C}{4} \frac{1}{1}, \quad 2 = \sum_{A2}^P = \frac{1+C}{16} \frac{2}{1}$; (b) For $C > C_2, p_2 = p_2^P = \underline{p_2}(1,C), \quad 2 = \sum_{A2}^P = \frac{C(1+C)(1-C^2)}{2(C^2-3C+4)^2} \frac{2}{1}$.

Figure 1 illustrates the second-period price scheme in the protonaximizing equilibrium. For $C \ 2 \ [0; C_3]$, the price $\underline{p_2}(\ _1; C)$, which is the minimum price that prevents the counterfeiter from mimicking the branded rm, has an inverted-U shape with respect to C and is higher than the monopoly price in benchmark. The counterfeiter's prot in the pooling equilibrium increases faster with C than its prot in the separating equilibrium when C is close to $0.^8$. Therefore, the authentic rm is forced to increase the price in order to reduce competition and increase the competitor's prot in the separating equilibrium. As C gets larger, the condition will be reversed and the authentic rm has no need to incur a large distortion to support the separating equilibrium. Combining these two segments give us an inverted-U shape price in the separating equilibrium. When $C \ 2 \ (C_3; C_2]$, the price increases with C because of higher expected quality. When C is close to 1, the game converges to Bertrand Competition of homogeneous good, and the price goes down to 0.

3.2 The Dynamic Game

In this subsection, I will analyze the dynamic game and illustrate why the entry of counterfeiter may generate higher prot for the incumbent. Given the second-period consumer surplus and the rst-period price, the marginal buyer in the rst period will be determined. The authentic rm's decision is to choose this marginal consumer to maximize total prot.

⁸When **C** is close to 0; $\frac{d \frac{P}{C2}}{dC} = \frac{1}{(1+C)^2} p_{A2}^2$ $\frac{d \frac{S}{C2}}{dC} = \frac{1}{4(1+C)^2} p_{A2}^2$.

The authentic rm's maximization problem is:

$$\max_{1} P_{A}(1) = (1 1)(2 1 \frac{1+C}{2} + p_{2}^{P}) + \frac{1}{2}(1 \frac{2p_{2}^{P}}{1+C})p_{2}^{P}$$

The marginal buyer ${}_{1}^{P}$ and equilibrium prot ${}_{A}^{P}$ are:

$$P_{1}^{P} = \frac{8}{1 + \frac{3}{2} \frac{C}{(1 + \frac{11}{16})}} \frac{3}{F} \frac{1}{F} \frac{1}{2} 11.9552 \text{ Tf} 16.054 \text{ } 3.12668 \text{ Td} (1)]TJ/F14 \text{ } 11.3552}{S}$$

producer, the branded rm takes a larger share of the total pro t compared to the head-to-head competition in the pooling equilibrium. The mechanism of the front-loading e ect is slightly di erent. Consumers will not be fooled ex post but face a super monopoly price in the second period as Lemma 2 indicated. Now, the marginal buyer $\frac{P}{1}$ faces two options in the second period | buy the authentic good or the counterfeit.

$$2_1 \quad p_1 = maxf_1 \quad \underline{p}_2(C; 1); C_1 \quad \frac{C}{2}\underline{p}_2(C; 1)g$$

However, the buyer who is indi erent between a genuine product and a counterfeit in the second period must below $_1$. Therefore, the outside option is purchasing the authentic good in t=2. The incumbent's pro t maximization is as follow.

$$\max_{1} A(1) = (1 1)(1 + \underline{p_2}(C; 1)) + A_2(1)$$

In equilibrium,

$$\begin{split} S_{1} &= \frac{1 + \frac{2(1 \ C^{2})}{C^{2} \ 3C + 4}}{2[1 + \frac{2(1 \ C^{2})(C^{2} + C + 2)}{(C^{2} \ 3C + 4)^{2}}]} \\ S_{A} &= \frac{[1 + \frac{2(1 \ C^{2})}{C^{2} \ 3C + 4}]^{2}}{4[1 + \frac{2(1 \ C^{2})(C^{2} + C + 2)}{(C^{2} \ 3C + 4)^{2}}]} \end{split}$$

The left segment of lower curve in Figure 2 informs that $\frac{S}{1}$ monotonically decreases with *C*. As the quality gap closes, the branded rm's pro t in the second period decreases. It would be better to assign less weight in the second period by decreasing $\frac{S}{1}$.

Pro t Comparison

Proposition 1. In the prot-maximizing equilibrium, the authentic rm's prot will be higher than the monopoly benchmark if the counterfeit quality is succently low ($C < C_4$ 0.188). When the counterfeit quality is above that threshold, at any equilibrium in the second period, competition always decreases the incumbent's pro t.

Figure 3 illustrates Proposition 1: when the pooling equilibrium emerges in the second period, the competition e ect is too strong and always dominates the front-loading e ect. The authentic rm su ers from the counterfeit entry. In the rst segment of the pooling equilibrium, the front-loading e ect gets weaker when the quality increases ($\frac{P}{1}$ increases with *C*) and the time-inconsistency problem is re-inforced. However, the high-quality counterfeit also weakens the competition e ect and raises the second-period pro t. In the second segment, the competition e ects gets too strong and the front-loading e ect disappears.

However, if the separating equilibrium is sustained, the branded rm's prot has

In the monopoly benchmark, total surplus is given by the following equation.

$$TS^{M} = \begin{bmatrix} Z_{1} & Z_{M} \\ 2 & d \end{bmatrix} + \begin{bmatrix} Z_{M} \\ 1 \\ \frac{M}{2} \end{bmatrix} d$$

The rst (second) term represents the surplus created by rst (second) period transaction⁹. The total surplus decreases with ₁, which is implied by the fact that early buyer enjoy double surplus. Given the marginal buyer in each period, $TS^{M} = 0.775$.

The welfare in the presence of deceptive counterfeit competition is a piecewise function.

$$TS(C) = \frac{\binom{8}{5}}{TS^{P}(C)} = \frac{\binom{8}{5}}{\binom{1}{2}} 2 \frac{d}{2} + \frac{\binom{8}{5}}{\binom{1}{-5}} \frac{d}{2} + \frac{\binom{8}{5}}{\binom{2}{-2}} C \frac{d}{2} \quad \text{if } C C_{3}$$

$$\xrightarrow{7S(C)} TS^{P}(C) = \frac{\binom{8}{5}}{\binom{1}{2}} 2 \frac{d}{2} + \frac{\binom{8}{5}}{\binom{2}{2}} \frac{1+C}{2} \frac{d}{2} \quad \text{if } C > C_{3}$$

typical criticism against counterfeits. However, if the rst-period welfare is taken into account, the result will be quite di erent. As Figure 2 shows, there are always more sales in t = 1 once C > 0. The front-loading e ect pushes consumers to buy in t = 1 either because the higher price or lower expected quality in t = 2. The The left segment is the welfare in the separating equilibrium. In Figure 2, as the counterfeit quality improves, the positive e lect increases with *C* roughly at the same speed ($\frac{d^2}{dC^2}$ is close to 0). The second-period welfare decreases because of upward distorted prices. Since the second-period price has an inverted-U shape, the welfare in that period will be an U shape curve. Combining these two e lects, it is clear why total welfare also has a U shape. When the counterfeit quality is 0, the model coincides with the benchmark. When *C* is small, unlike the pooling equilibrium, 1 is close to the benchmark value and decreases slower compared to the second-period welfare. Therefore, when the counterfeit quality is su ciently low, the overall welfare e lect is negative.

This proposition implies that deceptive counterfeits may have a positive e ect on welfare in a dynamic context, which is contrary to the traditional argument. What is more surprising is that welfare is signi cantly higher when counterfeits are indistinguishable ex post. The result reminds us to think deeply about the counterfeit problem. Firstly, branded rms actively adopt strategies against clones. Although counterfeits are deceptive ex ante, whether they can be recognized ex post is endogenized. If the quality of clones is low, in which case consumer confusion induced by counterfeits has a strong negative e ect on welfare, the authentic rm will signal by price and rational consumer will not be fooled. If consumers cannot distinguish counterfeits from authentic goods ex post, it must be that the quality gap is close enough. Even if consumers are diverted to counterfeits in that case, the welfare loss is relatively small. Secondly, consumers respond rationally to the problem. In the present paper, they are aware that surplus associated with future purchase is lowered by the counterfeit competition. Thus, more people buy earlier, which is bene cial for both the branded rm and welfare. However, as I point out, when the authentic rm decides to separate itself by distorted price, the counterfeiter

can also charge a higher price in the second period. This \price collusion" created by quality signaling might decrease welfare.

4 Equilibrium Re nement and Robustness

The pro t-maximizing equilibrium discussed above is only one of equilibria in our model. In this section, the Intuitive Criterion (Cho and Kreps, 1987) is applied to re ne equilibria. Since there are two signal senders here, I will use a competitive version as Bontems et al. (2005) and Yehezkel (2008). We will show that all pooling equilibria are eliminated with a tiny adjustment. The re nement is not applicable to separating equilibria because both rms' prices are informative.¹⁰ However, it is proved that our general conclusion that counterfeit competition may increase the branded rm's pro t and social welfare holds in all separating equilibria.

In previous discussion, both rms are assumed to have zero marginal cost. Now, let the authentic rm has a slightly higher marginal cost > 0 which is arbitrarily close to 0. This is just a tie-breaker that helps us to eliminate all pooling equilibria. By continuity of all functions in the paper, this modi cation will not alter any of our results except for the existence of pooling equilibria. For convenience, I only explicitly state this adjustment in the re nement.

¹⁰The Intuitive Criterion requires unilateral deviation. However, since the other rm charges the equilibrium price, consumers can use that information to construct the out of equilibrium belief. Therefore, I cannot simply assume a belief towards the deviating rm while the other one prices at the equilibrium path. Bester and Demuth (2011), Bontems et.al (2006) and Hertzendorf and Overgaard (2001) have discussed this issue.

4.1 Equilibrium Re nement

Pooling Equilibrium

The basic logic of the Intuitive Criterion is equilibrium dominance: an equilibrium should be eliminated if there exists an out-of-equilibrium price such that given consumer's most favorite belief, one type of rm would be better o by deviating from the equilibrium price to that out-of-equilibrium price, while the other type of rm cannot bene t from such deviation.

In terms of pooling equilibria, the Competitive Intuitive Criterion requires that there is no p^{0} , such that

$$_{A_2}(p^0; p_2^P; 1) \qquad _{A_2}(p_2^P; p_2^P; \frac{1}{2})$$
 (3)

$$_{C2}(p_2^P;p^0;1) < _{C2}(p_2^P;p_2^P;\frac{1}{2})$$
 (4)

However, for every pooling equilibrium, there must exist a p° such that both equations hold, which means all pooling equilibria are eliminated. The reason is similar to the re nement in the monopoly signaling game: The authentic rm with a higher marginal cost , no matter how small it is, has a lower cost to signal its quality. Since the the pro t function satis es single-crossing property, I can always nd an upward distorted price such that the authentic rm is willing to deviate to that price if consumers believe its high quality, while the counterfeiter is not willing to deviate even if people believe it produces genuine products at that price. The detail can be found in Proof of Proposition 3.

Separating Equilibrium

Since the Intuitive Criterion cannot be applied to separating equilibria, Hertzendorf and Overgaard (2001) and Yehezkel (2008) use a stronger re nement named Resistance to Equilibrium Defections (REDE) to select the unique and most intuitive separating equilibrium in the duopoly signaling game, which is similar to the unprejudiced equilibrium in Bagwell and Ramey (1991).¹¹ Only the least distorted equilibrium survives that re nement, which is the pro t-maximizing equilibrium investigated in the previous section. However, we don't need to impose that extra re nement since our main results hold in all separating equilibria, which is proved in next subsection. the counterfeit quality is below C_4 , the authentic rm's prot is always higher with the presence of counterfeits, no matter which separating equilibrium emerges in the second period.

In terms of the impact on welfare, there is not such a nice monotonicity property

among equilibria because the welfare in t = 2 may be too low when the price is secon93(termi)-333(uition9(257)-292(58pact) 125726 12

Exchange.

Firstly, the incumbent has no incentive to provide an inferior good in the second period. Deneckere and MacAfee (1996) points out the linear utility function fails the condition that damaged goods help to raise pro t. In my model, no matter what inferior quality the branded rm chooses, the optimal decision is to sell zero damaged version in t=2. The second-period price and pro t are the same as monopoly benchmark. Since the price is not higher than the monopoly price, the front-loading e ect does not exist. Therefore, the total pro t can never be higher than the benchmark. If there is any xed cost associate with product line introduction, the pro t is always lower than the monopoly case.

Secondly, damaged goods introduced in the Iteriod.-335(in)-334(not)-3335pro t la iall dHahence014ttroducengods inodmadel, paeri,-3039part-4017(of-2016higgh-4017(0501I)28(vw Ind HwerewitDhe-3247ond28(t)ntuous-2346rondsumrs-TJ 0 -21.669 Td [(m)27(y)p-27(e),-332

5 Conclusion

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competition is intense. The unconstrained optimal is higher than $\underline{p_2}(_1; C)$. Since the prot function is a concave parabola as well, $p_2^P = \underline{p_2}(_1; C)$.

As Lemma 1 indicates, when $C = C_1$, both types of equilibria exist and $_{A2} = Max \ f \ _{A2}^S; \ _{A2}^Pg.$ Given $C_1 < C_2$, the price of the optimal pooling equilibrium is $p_2^P = \frac{1+C}{4}$. Since $\frac{d \ _{A2}^S}{dC} < 0$ and $\frac{d \ _{A2}^P}{dC} > 0$, there is a cut-o quality $C_3 = 0.512$ such that the optimal separating equilibrium is chosen if $C = C_3$ and the pooling equilibrium would be selected for $C_3 < C = C_1$. 2V hen the counterfeit quality is 0

If
$$p_2^P = \frac{1+C}{4}$$
,

$$\frac{d \frac{P}{A}}{dC} = \frac{(1 + \frac{3-C}{4})(2 + \frac{35C-53}{64})}{(1 + \frac{11-5C}{16})^2} < 0, 8C \ 2 \ (C_3, 1)$$
Therefore, $8C = C_3, \frac{P}{A} \ (C) = \frac{P}{A} \ (C_3)$. Since $\frac{P}{A} \ (C_3) < \frac{M}{4}$, we have $\frac{P}{A} \ (C) < \frac{P}{A} \ (C) < \frac{P}{A}$

^M, 8C C₃.

(2) When $C = C_3$, the separating equilibrium is supported in the second period. If C = 0, the model is degenerated to the monopoly benchmark. $M = \frac{S}{A}$. Let $(C) = \frac{S}{A} = \frac{M}{A}$, then total welfare. When $p_2^P = \frac{1+C}{4}_{1,} p_2^P = \frac{1}{2} p_1^P$.

$$TS^{P}(C) = \frac{Z_{1}}{P_{1}} 2 d + \frac{Z_{P_{1}}}{P_{2}} \frac{1+C}{2} d$$
$$= 1 (\frac{P}{1})^{2} (1 - \frac{3(1+C)}{16})$$
$$TS^{P}(C) = TS^{P}(C) - TS^{M}(C) = \frac{5}{8} (\frac{M}{1})^{2} - (\frac{P}{1})^{2} (1 - \frac{3(1+C)}{16})$$
$$\frac{d - TS^{P}(C)}{dC} = \frac{8(1+C)}{(27 - 5C)^{3}} > 0$$

Therefore, $TS^{P}(C)$ $TS^{P}(C_{3})$, $8C > C_{3}$. Since, $TS^{P}(C_{3}) > 0$, deceptive counterfeits always yield a higher welfare under the pooling equilibrium.

(2) In the separating equilibrium,

$$\frac{-S}{2} = \frac{2}{2(1-C)} \frac{P_2}{P_2} (C_{i-1}) \frac{1}{2} \frac{0}{2} \mu$$

 $_{A2}(p;p;\frac{1}{2})$ and $_{A2}(p + (1 \quad C)_{1};p;1) = 0 < _{A2}(p;p;\frac{1}{2})$. Therefore, by the continuity of prot function, there must exist a $p < p^0 < p + (1 \quad C)_1$ that makes $_{A2}(p^0;p;1) = _{A2}(p;p;\frac{1}{2})$.

Plug p° and Eq(3) into Eq(4),

$$C_{2}(p;p^{0};1) = C_{2}(p;p;\frac{1}{2})$$

$$= (1 \frac{p^{0}}{1} \frac{p}{C})p^{0} \frac{1}{2}(1 \frac{2p}{1+C})p^{0}$$

$$= (1 \frac{p^{0}}{1} \frac{p}{C})(\frac{p}{p}) < 0$$

Hence, for every pooling equilibrium, there is a price p^0 that the authentic rm wants to deviate and the counterfeiter does not given consumer's best belief.

Now let's make some preliminary de nition for separating equilibria

<u>p2</u>(C6(b1552 0 ()]TJ/F36 11.9552 Tf2 9.211.676 -1.794 T1 [(2)]TJ/F17 11.9552

Since 1 $\frac{2}{2(1-C)}K(C)$ 1 $\frac{2}{2(1-C)}\overline{K}(C) > 0$, $\frac{@ \int_{A}^{S}}{@K(C)} > 0$. The protomaximizing equilibrium is the one that yields lowest total prot for the incumbent. In that equilibrium, when C C_4 , the protomatic with counterfeit entry is higher. Therefor no matter which separating equilibrium is sustained in the second period, $\int_{A}^{S}(C) = 0$ if C C_4 .

(iii) For total welfare:

When C = 0,

$$TS^{S}(C; K(C)) = 0.225 \quad \frac{1}{8} \frac{[1 + K(C)]^{2}[1 + \frac{4 - 3C}{4 - 4C}K(C)^{2}]}{[1 + \frac{2 - C}{2 - 2C}K(C)^{2}]^{2}}$$
$$TS^{S}(0; K(0)) = 0.225 \quad \frac{1}{8}$$