entations for a triangle or a pentagon with ensu-
ing $\mathbf{n(r)}$ having at least two planes of mirror
symmetry: (i) one with a side along $\mathbf{n_0}$ giving an

Supporting Online Material

Shape Controlled Colloidal Interactions in Nematic Liquid Crystals

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calculated in real time and relayed to the spatial

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and strength of surface anchoring. The symmetry of $\mathbf{n}(\mathbf{r})$ does not change when either surface anchoring or size of an odd-N platelet such as a triangle is reduced (Figs. S1D and E); the deformations are smaller, and therefore, the magnitude of $\mathbf{p}$ is smaller than in the strong anchoring case, but the $\mathbf{n}(\mathbf{r})$ structure remains dipolar. This behavior is similar to the case of spherical colloids with planar surface anchoring retaining their quadrupolar symmetry of $\mathbf{n}(\mathbf{r})$ with varying the particle size and anchoring strength (Figs. S1J and K).

The above differences between the behavior of spherical and anisotropic colloids can be understood by considering the bulk elastic and surface anchoring energy associated with introducing the colloidal inclusions into the NLC. The Frank elastic energy of NLCs can be expressed in terms of spatial gradients of $\mathbf{n}(\mathbf{r})$:

$$U[\mathbf{n}(\mathbf{r})] = \int d^3\mathbf{r} \left[K_{11}(\nabla \cdot \mathbf{n})^2 + K_{22}(\mathbf{n} \cdot \nabla \times \mathbf{n})^2 + K_{33}(\mathbf{n} \times \nabla \times \mathbf{n})^2 \right] \tag{S1}$$

where K_{11}, K_{22}, and K_{33} are three independent Frank elastic constants corresponding to !splay", !bend", and !twist" deformations respectively (*S18*) and the integration is carried out over the volume of the NLC. The three elastic constants of thermotropic small molecule nematics are of the same order of magnitude [e.g. for 5CB at room temperature K_{11} é 6.4 pN, K_{22} é 3 pN, and K_{33} é 10 pN (*S19*)]. In the one elastic constant approximation, Eq. (S1) is often approximated as

$$U = K \int d^3\mathbf{r} (\nabla \mathbf{n})^2$$

over the surface area of the platelet. For finite anchoring strength, the $\mathbf{n}(\mathbf{r})$ configuration that occurs for a given colloid is the one that minimizes the total energy including both the bulk Frank elastic and surface anchoring terms: $U_{tot} = U_{el} + U_S$; whereas in the strong anchoring limit (w, $\mathbf{w}$, one minimizes only U_{el} with fixed boundary conditions for $\mathbf{n}(\mathbf{r})$ on the surface of the colloid. Different than th

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Particle displacements along and perpendicular to $\mathbf{n_0}$ ($\delta_\parallel$ and $\delta_\perp$, respectively) over various delay times τ were extracted from the trajectory data shown in Fig. S3A. Histograms sampled from the time-delayed displacements are well described by Gaussian distributions with different widths or mean-square displacements, $\sigma^2_{\parallel,\perp}$ (Fig. S3B). As is shown in Fig. S3C, the two mean-square

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Fig. S1. Effects of surface anchoring and particle size on the symmetry of director structures induced by colloids. For spheres with vertical surface anchoring, reducing their size or weakening the surface anchoring changes the symmetry of **n**

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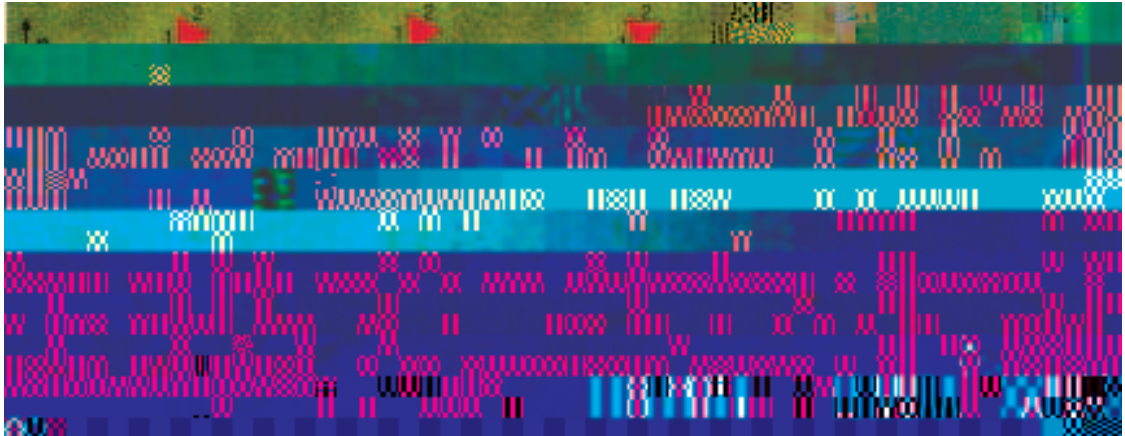**Fig. S3.** Drag coefficients of a colloidal square in 5CB via diffusion measurements. (**A**) Blue points show the trajectory of the square in the background image determined from a video of total duration 1000 sec acquired at a frame rate of 15 Hz. The double-headed arrow shows the far-field alignment direction $\mathbf{n_0}$. (**B**) Histograms for displacements along the x-direction (circles) and the y-direction (squares) extracted from the trajectory data in (A) with sampling time delays of $\tau = 0.33$ sec (top) and $\tau = 1.5$ sec (bottom). Black lines show Gaussian fits to the histograms. (**C**) Mean square displacement $q_\parallel^2$ parallel to $\mathbf{n_0}$ (circles) and $q_\perp^2$ perpendicular to $\mathbf{n_0}$ (squares) as a function of τ. Slopes determined with linear fits to the data give values of the two diffusion

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