

of a laser frequency comb. This represents the first $f-2f$ stabilization of a frequency comb using a single amorphous material and demonstrates how photonic waveguides can serve as an appealing platform for both ⁽²⁾ and ⁽³⁾

If the separated charges can be stabilized at trap sites or defects in the material, then the static electric field will induce a $\chi^{(2)}$ in the material that oscillates sinusoidally along the waveguide length with the correct period to quasi-phase-match SHG. The generated second-harmonic light interferes with the fundamental to produce more charge separation, which, in turn, enables stronger SHG. This positive feedback continues until the process saturates.

Group-velocity matching. In contrast to previous studies of photoinduced SHG in SiN waveguides^{9,10}, which observed SHG in any waveguide, regardless of geometry, we only generate the second harmonic across a small range of waveguide widths. This difference is

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